

APPLICATION NO. 10/772,597

INVENTION: Decisioning rules for turbo and convolutional decoding

INVENTORS: Urbain A. von der Embse

Currently amended CLAIMS

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CLAIMS

WHAT IS CLAIMED IS:

10 Claim 1. (currently amended) A ~~means~~ method for the
performing a new turbo decoding algorithm using a-posteriori
probability $p(s, s' | y)$ in equations (13) ~~of the invention~~
~~disclosure of the decoder trellis states s', s for the received~~
~~codeword $k-1, k$ conditioned on the received symbol set $y =$~~
15 ~~$\{y(1), y(2), \dots, y(k-1), y(k), \dots, y(N)\}$ for defining the maximum~~
a-posteriori probability MAP, comprising: in turbo decoding and
which comprises:

using a new statistical definition of the MAP logarithm
likelihood ratio $L(d(k) | y)$ in equations (18)

20

$$L(d(k) | y) = \ln[\sum_{(s, s' | d(k)=+1)} p(s, s' | y)] \\ - \ln[\sum_{(s, s' | d(k)=-1)} p(s, s' | y)]$$

25

equal to the natural logarithm of the ratio of the a-
posteriori probability $p(s, s' | y)$ summed over all state
transitions $s' \rightarrow s$ corresponding to the transmitted data
 $d(k)=1$ to the $p(s, s' | y)$ summed over all state transitions
 $s' \rightarrow s$ corresponding to the transmitted data $d(k)=0$,

using a factorization of the a-posteriori probability $p(s, s' | y)$

30

in equations 13 into the product of the a-posteriori
probabilities $p(s' | y(j < k)), p(s | s', y(k)), p(s | y(j > k))$

$$p(s, s' | y) = p(s | s', y(k)) p(s | y(j > k)) p(s' | y(j < k)),$$

using a turbo decoding forward recursion equation for evaluating
~~— said a-posteriori probability $p(s'|y(j < k))$ using said~~
~~— $p(s|s', y(k))$ as the state transition a-posteriori~~
5 ~~— probability of the trellis~~

$$p(s|y(j < k), y(k)) = \sum_{\text{all } s'} p(s|s', y(k)) p(s'|y(j < k))$$

for evaluating said a-posteriori probability $p(s'|y(j < k))$
10 in equations 14 using $p(s|s', y(k))$ as the state transition
a-posteriori probability of the trellis transition path
 $s' \rightarrow s$ to the new state s at k from the previous state s' at
 $k-1$ and given the observed symbol $y(k)$ to update these
recursions for the assumed value of the user data bits $d(k)$
15 equivalent to the transmitted symbol $x(k)$ which is the
modulated symbol corresponding to $d(k)$,

using a turbo decoding backward recursion equation for evaluating
~~— said a-posterior probability $p(s|y(j > k))$ using said~~
~~— $p(s'|s, y(k))$ as the state transition a-posteriori~~
20 ~~_____~~

$$p(s'|y(j > k-1)) = \sum_{\text{all } s} p(s|y(j > k)) p(s'|s, y(k))$$

for evaluating the a-posterior probability $p(s|y(j > k))$ in
equations 15 using said $p(s'|s, y(k)) = p(s|s', y(k))$ as the
25 state transition a-posteriori probability of the trellis transition pa
equivalent to said transmitted symbol $x(k)$ which is the
modulated symbol corresponding to said $d(k)$ and where said
 $p(s'|s, y(k)) = p(s|s', y(k))$,

evaluating the natural logarithm of the state transition a-
30 posteriori probability $p(s|s', y(k)) = p(s'|s, y(k))$ as a
~~— function which is linear in the received symbol~~
 $y(k)$ equal to the new decisioning metric DX in equations
11, 16, defined by equation

$$\begin{aligned}
 \ln[p(s|s', y(k))] &= \ln[p(s'|s, y(k))] \\
 &= \text{Re}[y(k)x^*(k)]/\sigma^2 - |x(k)|^2/2\sigma^2 + p(d(k)) \\
 &= DX
 \end{aligned}$$

5 ~~and wherein~~ p is the natural logarithm \ln of p , x^* is the complex conjugate of x , and $\ln[o]$ is the natural logarithm of $[o]$;

evaluating said natural logarithm of said state transition a-posteriori probability $p(s'|s, y(k))$ equal to
 10 the new decisioning metric DX in equations (11), (16)

$$\begin{aligned}
 \ln[p(s|s', y(k))] &= \ln[p(s'|s, y(k))] \\
 &= \text{Re}[y(k)x^*(k)]/\sigma^2 - |x(k)|^2/2\sigma^2 + p(d(k)) \\
 &= DX
 \end{aligned}$$

15 ~~and which is linear in said received symbol $y(k)$,~~
 whereby said new state transition probabilities in said MAP equations use said DX linear in $y(k)$ in place of the current use of the maximum likelihood decisioning metric
 20 $DM = [-|y(k) - x(k)|^2/2\sigma^2]$ which is a quadratic function of $y(k)$,

$$DM = [-|y(k) - x(k)|^2/2\sigma^2],$$

25 ~~which is a quadratic function of $y(k)$,~~
 whereby said MAP turbo decoding algorithms ~~realizes~~ provide some of the performance improvements demonstrated in FIG. 5, 6 using said DX , and
 said whereby this new a-posteriori mathematical framework enables
 30 said MAP turbo decoding algorithms to be restructured and to determine the intrinsic information as a function of said DX linear in said $y(k)$.

Claim 2. (currently amended) ~~Wherein in claim 1 a~~ A method for performing means for said a new convolutional decoding algorithm in said using the MAP a-posteriori probability $p(s, s' | y)$ and which comprises in equations 13, comprising::

5 using a new maximum a-posteriori principle which maximizes the a-posteriori probability $p(x|y)$ of the transmitted symbol x given the received symbol y to replace the current maximum likelihood principle which maximizes the likelihood probability $p(y|x)$ of y given x for deriving the forward and the backward recursive equations to implement convolutional decoding,

10 using ~~said the~~ factorization of ~~said the~~ a-posteriori probability $p(s, s' | y)$ in equations 13 into the product of said a-posteriori probabilities $p(s' | y(j < k))$, $p(s | s', y(k))$,
15 $p(s | y(j > k))$ to identify the convolutional decoding forward state metric $a_{k-1}(s')$, backward state metric $b_k(s)$, and state transition metric $p_k(s | s')$ as the a-posteriori probability factors

$$\begin{aligned} p_k(s | s') &= p(s | s', y(k)) \\ b_k(s) &= p(s | y(j > k)) \\ a_{k-1}(s') &= p(s' | y(j < k)), \end{aligned}$$

20 using a convolutional decoding forward recursion equation in
25 equations 14 for evaluating said a-posteriori probability $a_k(s) = p(s | y(j < k), y(k))$ using said $p_k(s | s') = p(s | s', y(k))$ as said state transition probability of the trellis transition path $s' \rightarrow s$ to the new state s at k from the previous state s' at $k-1$,

30 using a convolutional decoding backward recursion equation in equations 15 for evaluating said a-posteriori probability $b_k(s) = p(s | y(j > k))$ using said $p_k(s' | s) = p(s' | s, y(k))$ as said state transition probability

of the trellis transition path $s \rightarrow s'$ to the new state s' at $k-1$ from the previous state s at k ,
evaluating the natural logarithm of said state transition
a-posteriori probabilities

$$\begin{aligned} \ln[p_k(s'|s)] &= \ln[p(s'|s, y(k))] \\ &= \ln[p(s|s', y(k))] \\ &= \ln[p_k(s|s')] \\ &= DX \end{aligned}$$

equal to ~~said~~ the new decisioning metric DX in equations
16, and
implementing said convolutional decoding algorithms to
realize obtain some of the performance improvements
demonstrated in FIG. 5, 6 using said DX .

Claim 3. (currently amended) Wherein in claim ~~12~~ ~~A means~~
~~for a~~ method for implementing the new convolutional decoding
recursive equations, ~~which calculate said MAP a-posteriori~~
~~probability $p(s, s'|y)$ said method comprising: and which comprises:~~
~~said implementing in equations 14 a forward recursion equation~~
for evaluating ~~said the~~ natural logarithm, a_k , of a_k using
~~said $p_k = \ln[p(s|s', y(k))]$ as the natural logarithm said of~~
the state transition a-posteriori probability
 $p_k = \ln[p(s|s', y(k))]$ of the trellis transition path $s' \rightarrow s$ to
the new state s at k from the previous state s' at $k-1$,
which is equation and is

$$\begin{aligned} \underline{a}_k(s) &= \max_{s'} [\underline{a}_{k-1}(s') + p_k(s|s')] \\ &= \max_{s'} [\underline{a}_{k-1}(s') + DX(s|s')] \\ &= \max_{s'} [\underline{a}_{k-1}(s') + \text{Re}[y(k)x^*(k)]/\sigma^2 - |x(k)|^2/2\sigma^2 + p(d(k))] \end{aligned}$$

wherein said $DX(s|s') = p_k(s|s') = p_k(s'|s) = DX(s'|s) = DX$ is said
 the new decisioning metric, and
 said implementing in equations 15 a backward recursion equation
 for evaluating said the natural logarithm, b_k , of b_k using
 5 said $p_k = \ln[p(s'|s, y(k))] = \ln[p(s|s', y(k))]$ as the natural
 logarithm of said state transition a-posteriori probability
 $p_k = \ln[p(s'|s, y(k))] = \ln[p(s|s', y(k))]$ of the trellis
 transition path $s \rightarrow s'$ to the new state s' at $k-1$ and is
 equation

$$b_{k-1}(s') = \max_s [b_k(s) + DX(s'|s)] \text{ and,}$$

said decoding algorithms realize some of the
 performance improvements demonstrated in FIG. 5, 6 using said
 15 DX .